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MATDIP301

Third Semester B.E. Degree Examination, December 2011

Advanced Mathematics - I

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions.

- 1 a. Express $\frac{1}{(2+i)^2} - \frac{1}{(2-i)^2}$ in the form $a + ib$. (06 Marks)
- b. Find the modulus and amplitude of $\frac{(3-\sqrt{2}i)^2}{1+2i}$. (07 Marks)
- c. Find the real part of $\frac{1}{1+\cos\theta+i\sin\theta}$. (07 Marks)
- 2 a. Find the n^{th} derivative of $\cos x \cos 2x \cos 3x$. (06 Marks)
- b. If $y = (\sin^{-1} x)^2$, show that $(1-x^2)y_{n+2} - (2n+1)xy_{n+1} - n^2y_n = 0$. (07 Marks)
- c. Find the n^{th} derivative of $\frac{x+2}{x+1} + \log\left(\frac{x+2}{x+1}\right)$. (07 Marks)
- 3 a. State and prove Euler's theorem. (06 Marks)
- b. Given $u = \sin\left(\frac{x}{y}\right)$, $x = e^t$, $y = t^2$, find $\frac{du}{dt}$ as a function of t . (07 Marks)
- c. If $x = r \cos \theta$, $y = r \sin \theta$, find $\frac{\partial(x,y)}{\partial(r,\theta)}$ and $\frac{\partial(r,\theta)}{\partial(x,y)}$. (07 Marks)
- 4 a. Find the angle of intersection of the curves $r = a(1 + \cos \theta)$ and $r = b(1 - \cos \theta)$. (06 Marks)
- b. Find the pedal equation of the curve $\frac{2a}{r} = 1 - \cos \theta$. (07 Marks)
- c. Expand $e^{\sin x}$ by Maclaurin's series upto the term containing x^4 . (07 Marks)
- 5 a. Obtain the reduction formula for $I_n = \int_0^{\frac{\pi}{2}} \sin^n x \, dx$ where n is a positive integer. (06 Marks)
- b. Evaluate: $\int_1^5 \int_1^{x^2} x(x^2 + y^2) \, dx \, dy$. (07 Marks)
- c. Evaluate: $\int_0^1 \int_0^2 \int_0^2 x^2 yz \, dx \, dy \, dz$. (07 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
2. Any revealing of identification, appeal to evaluator and/or equations written eg, $42+8 = 50$, will be treated as malpractice.

- 6 a. Prove that $\beta(m, n) = \frac{\Gamma(m)\Gamma(n)}{\Gamma(m+n)}$. (06 Marks)
- b. Show that $\Gamma(n) = \int_0^1 \left(\log \frac{1}{x}\right)^{n-1} dx$. (07 Marks)
- c. Express $\int_0^{\pi/2} \sqrt{\tan \theta} d\theta$ in terms of Gamma function. (07 Marks)
- 7 a. Solve: $\frac{dy}{dx} = \frac{x(2 \log x + 1)}{\sin y + y \cos y}$. (06 Marks)
- b. Solve: $(1 + e^{xy})dx + e^{xy} \left(1 - \frac{x}{y}\right)dy = 0$. (07 Marks)
- c. Solve: $(x^2 - ay)dx = (ax - y^2)dy$. (07 Marks)
- 8 a. Solve: $\frac{d^4 y}{dx^4} + 8 \frac{d^2 y}{dx^2} + 16y = 0$. (06 Marks)
- b. Solve: $(D - 2)^2 y = 8(e^{2x} + \sin 2x)$. (07 Marks)
- c. Solve: $(D^3 + 4D)y = \sin 2x$. (07 Marks)

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10MAT/PM/TL/MA31

Third Semester B.E. Degree Examination, December 2011
Engineering Mathematics – III

Time: 3 hrs.

Max. Marks:100

- Note: 1. Answer any FIVE full questions, selecting at least TWO questions from each part.**
2. Missing data will be suitably assumed.

PART – A

- 1 a. Obtain the Fourier series for the function $f(x) = \begin{cases} \pi x & : 0 \leq x \leq 1 \\ \pi(2-x) & : 1 \leq x \leq 2 \end{cases}$ and deduce that

$$\frac{\pi^2}{8} = \sum_{n=1}^{\infty} \frac{1}{(2n-1)^2}. \quad (07 \text{ Marks})$$

- b. Obtain the half range Fourier sine series for the function. (07 Marks)

$$f(x) = \begin{cases} 1/4 - x & ; 0 < x < 1/2 \\ x - 3/4 & ; 1/2 < x < 1 \end{cases}$$

- c. Compute the constant term and the first two harmonics in the Fourier series of $f(x)$ given by the following table. (06 Marks)

x	:	0	1	2	3	4	5
f(x)	:	4	8	15	7	6	2

- 2 a. Find the Fourier transform of $f(x) = \begin{cases} 1-x^2 & \text{for } |x| \leq 1 \\ 0 & \text{for } |x| > 1 \end{cases}$ and hence evaluate

$$\int_0^{\infty} \left(\frac{x \cos x - \sin x}{x^3} \right) \cos \frac{x}{2} dx. \quad (07 \text{ Marks})$$

- b. Find the Fourier cosine transform of $f(x) = \frac{1}{1+x^2}$. (07 Marks)

- c. Solve the integral equation $\int_0^{\infty} f(\theta) \cos \alpha \theta d\theta = \begin{cases} 1-\alpha & ; 0 \leq \alpha \leq 1 \\ 0 & ; \alpha > 1 \end{cases}$. Hence evaluate $\int_0^{\infty} \frac{\sin^2 t}{t^2} dt$. (06 Marks)

- 3 a. Solve two dimensional Laplace equation $u_{xx} + u_{yy} = 0$, by the method of separation of variables. (07 Marks)

- b. Solve the one dimensional heat equation $\frac{\partial u}{\partial t} = c^2 \frac{\partial^2 u}{\partial x^2}$, $0 < x < \pi$ under the conditions :

i) $u(0,+) = 0, u(\pi, t) = 0$ ii) $u(x, 0) = u_0 \sin x$ where $u_0 = \text{constant} \neq 0$. (07 Marks)

- c. Obtain the D' Alembert's solution of one dimensional wave equation. (06 Marks)

- 4 a. Fit a curve of the form $y = ae^{bx}$ to the following data : (07 Marks)

x	:	77	100	185	239	285
y	:	2.4	3.4	7.0	11.1	19.6

- b. Using graphical method solve the L.P.P minimize $z = 20x_1 + 10x_2$ subject to the constraints $x_1 + 2x_2 \leq 40$; $3x_1 + x_2 \geq 0$; $4x_1 + 3x_2 \geq 60$; $x_1 \geq 0$; $x_2 \geq 0$. (06 Marks)

- c. Solve the following L.P.P maximize $z = 2x_1 + 3x_2 + x_3$, subject to the constraints $x_1 + 2x_2 + 5x_3 \leq 19$, $3x_1 + x_2 + 4x_3 \leq 25$, $x_1 \geq 0$, $x_2 \geq 0$, $x_3 \geq 0$ using simplex method. (07 Marks)

PART - B

- 5 a. Using the Regula - falsi method, find the root of the equation $xe^x = \cos x$ that lies between 0.4 and 0.6. Carry out four iterations. (07 Marks)
- b. Using relaxation method solve the equations :
 $10x - 2y - 3z = 205$; $-2x + 10y - 2z = 154$; $-2x - y + 10z = 120$. (07 Marks)
- c. Using the Rayleigh's power method, find the dominant eigen value and the corresponding eigen vector of the matrix. $A = \begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}$ starting with the initial vector $[1, 1, 1]^T$. (06 Marks)

- 6 a. From the following table, estimate the number of students who have obtained the marks between 40 and 45 : (07 Marks)

Marks	: 30-40	40-50	50-60	60-70	70-80
Number of students	: 31	42	51	35	31

- b. Using Lagrange's formula, find the interpolating polynomial that approximate the function described by the following table : (07 Marks)

x	: 0	1	2	5
f(x)	: 2	3	12	147

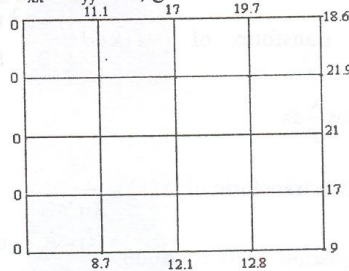
Hence find $f(3)$

- c. A curve is drawn to pass through the points given by the following table :

x	: 1	1.5	2	2.5	3	3.5	4
y	: 2	2.4	2.7	2.8	3	2.6	2.1

- Using Weddle's rule, estimate the area bounded by the curve, the x - axis and the lines $x = 1$, $x = 4$. (06 Marks)

- 7 a. Solve the Laplace's equation $u_{xx} + u_{yy} = 0$, given that : (07 Marks)



- b. Solve $\frac{\partial^2 u}{\partial t^2} = 4 \frac{\partial^2 u}{\partial x^2}$ subject to $u(0, t) = 0$; $u(4, t) = 0$; $u(x, 0) = x(4 - x)$. Take $h = 1$, $k = 0.5$. (07 Marks)

- c. Solve the equation $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$ subject to the conditions $u(x, 0) = \sin \pi x$, $0 \leq x \leq 1$; $u(0, t) = u(1, t) = 0$ using Schmidt's method. Carry out computations for two levels, taking $h = 1/3$, $k = 1/36$. (06 Marks)

- 8 a. Find the Z - transform of : i) $(2n-1)^2$ ii) $\cos\left(\frac{n\pi}{2} + \pi/4\right)$ (07 Marks)

- b. Obtain the inverse Z - transform of $\frac{4z^2 - 2z}{z^3 - 5z^2 + 8z - 4}$. (07 Marks)

- c. Solve the difference equation $y_{n+2} + 6y_{n+1} + 9y_n = 2n$ with $y_0 = y_1 = 0$ using Z transforms. (06 Marks)

- c. Explain common emitter, common collector amplifier along with its a.c. equivalent circuit. (04 Marks)

PART - B

- 5 a. Explain the classification of large signal amplifiers as class A, class B, class C and class AB amplifiers. (06 Marks)
- b. An amplifier with openloop voltage gain of 1000, delivers 10W of power output at 10% second harmonic distortion when i/p is 10 mV. A 40 dB negative feedback is applied and output power is to remain at 10W. Determine required input signal V_s and second harmonic distortion with feedback. (08 Marks)
- c. Explain the advantages and disadvantages of negative feedback. (06 Marks)
- 6 a. Explain with a neat diagram Hartley oscillator and colpits oscillate as LC oscillator. (06 Marks)
- b. Explain the various types of multivibrators. Also mention the applications. (06 Marks)
- c. Obtain the expression for time period T at the base of transistor, in case of wave shaping circuits. (08 Marks)
- 7 a. Explain with a functional block diagram, a typical three terminal IC voltage regulator. (06 Marks)
- b. Discuss the limitations of linear voltage regulators. (06 Marks)
- c. Briefly discuss power converters in series and parallel connection along with neat diagrams. (08 Marks)
- 8 a. Discuss the requirements of a good instrumentation amplifier. (06 Marks)
- b. Fig.Q.8(b) shows dual input, balanced output and differential amplifier configuration. Assuming silica transistor with $h_{ie} = 2.8 \text{ K}\Omega$, calculate : i) Operating point values ; ii) Differential gain ; iii) Common mode gain ; iv) CMRR ; v) Output if $V_{S1} = 70 \text{ mV}$ peak to peak at 1 kHz ; vi) $V_{S2} = 40 \text{ mV}$ peak to peak at 1 kHz. (10 Marks)

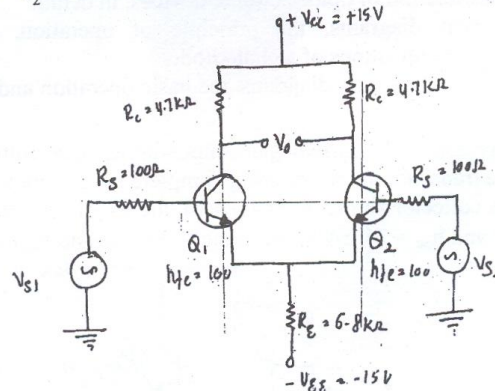


Fig.Q.8(b)

- c. Explain the various electrical characteristics of an op-amp which are generally in the data sheet. (04 Marks)

- 6 a. Mention any two differences between asynchronous and synchronous counter. With a neat block diagram, output waveforms and truth table. Explain a 3-bit binary Ripple Down-Counter constructed using negative-edge triggered JK flip-flops. (10 Marks)
- b. A 4-bit binary asynchronous counter is connected with a clock of 500 KHz frequency. Find the time period of the waveform at the output of the first and the last JK flipflop. (02 Marks)
- c. Design a synchronous mod-6 counter using JK flipflop. (08 Marks)
- 7 a. Compare Moore and Mealy model of synchronous sequential circuit. (06 Marks)
- b. Design an asynchronous sequential logic circuit for state transition diagram shown in Fig.Q7(b).

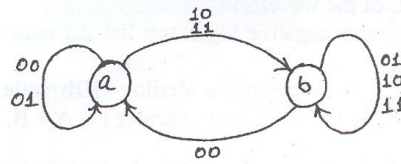


Fig.Q7(b)

(06 Marks)

- c. Reduce state transition diagram (Moore model) of Fig.Q7(c) by,
 i) Row elimination method ii) Implication table method.

(08 Marks)

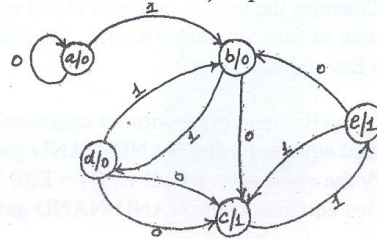


Fig.Q7(c)

- 8 a. Discuss the two drawbacks of resistive divider used in converting digital input to analog output. Draw the schematic for a 4-bit binary ladder and explain how the digital to analog conversion is achieved using it. (10 Marks)
- b. Using a schematic block diagram, briefly explain counter type ADC. (08 Marks)
- c. A counter type 10 bit ADC is connected with 7 MHz clock. Find :
 i) The average conversion time
 ii) The maximum conversion rate. (02 Marks)

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10CS36

Third Semester B.E. Degree Examination, December 2011
Object Oriented Programming with C++

Time: 3 hrs.

Max. Marks:100

**Note: Answer FIVE full questions, selecting
atleast TWO questions from each part.**

PART – A

- 1 a. Explain the terms encapsulation, polymorphism and inheritance in object oriented programming. (06 Marks)
- b. What is function overloading? Write a C++ program to define three overloaded functions area (), to find area of rectangle area of rectangular box and area of circle. (08 Marks)
- c. With an example explain the concept of inline functions. (06 Marks)

- 2 a. Differentiate between class and object. Write a C++ program to define a class called TIME with hour, minute and second as data members and read(), display() and add() as member functions. (10 Marks)
- b. What is a constructor? What are its characteristics? Define a suitable parameterized constructor with default values for the class box with data members length, breadth and height as data members. (10 Marks)

- 3 a. What is a friend function? Explain the need of friend functions in C++. (05 Marks)
- b. Write a C++ program to swap two integer and floating-point numbers, using a function template. (05 Marks)
- c. What is operator overloading? Write a C++ program to add two complex numbers by overloading the + operator. Also overload >> and << operators for reading and displaying the complex numbers. (10 Marks)

- 4 a. Explain the visibility of the base class members, for the access specifiers : private, protected and public while creating the derived classes. (06 Marks)
- b. Differentiate between private members and protected members. Write a C++ program to illustrate protected members in the base class. (07 Marks)
- c. With an example explain multiple inheritance. (07 Marks)

PART – B

- 5 a. With an example explain the order of invocation of constructors and destructors and passing arguments to base class constructors in multilevel inheritance. (10 Marks)
- b. What are the ambiguities that arise in multiple inheritance? How to overcome this? Explain with examples. (10 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
2. Any revealing of identification, appeal to evaluator and /or equations written eg. 42+8 = 50, will be treated as malpractice.

- 6 a. What is a virtual function? Explain with a suitable example. (06 Marks)
- b. Write a C++ program to create a base class called shape. Use this class to store two double type values that could be used to compute the area of figures. Derive two specific classes called triangle and rectangle from the base shape. Add to the base class, a member function called `get_data()` to initialize base class data members and another member function `display_area()` to compute and display the area of figures. Make `display_area()` as a virtual function and redefine this function in derived classes to suit their requirements. (08 Marks)
- c. Write a C++ program to create base class called number with an integer data member and a member function to set the value for this data member. Derive three classes from this base class called hexadecimal, decimal and octal. Include a member function `show()` in all these three derived classes to display the value of the base class data member in hexadecimal, decimal and octal respectively. Use the concept of pure virtual functions. (06 Marks)
- 7 a. With an example and general syntax explain the member functions :
- i) `width()`
 - ii) `precision`
 - iii) `fill()`. (06 Marks)
- b. Write a C++ program to define a class called phonebook with data members name, area code, prefix and number and the member functions `readdata()` which reads the values of the data members from the keyboard and `writedata()` which displays the values of the data members. Enter the data for at least 5 phone numbers and store details in a binary file phone and read the stored details and display on the screen. (09 Marks)
- c. Briefly explain the member functions : `setf()` and `unsetf()`. (05 Marks)
- 8 a. What is exception handling? Briefly explain the facilities in C++ for exception handling. (10 Marks)
- b. Briefly explain the use of containers, vectors, lists and maps in STL. (10 Marks)

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