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21MAT31

Third Semester B.E. Degree Examination, Dec.2023/Jan.2024 Transform Calculus Fourier Series & Numerical Techniques

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1
- a. Find the Laplace transform of, (i) $e^{-3t} \sin 5t \cdot \cos 3t$ (ii) $\frac{e^{at} - e^{bt}}{t}$. (06 Marks)
- b. If a periodic function of period 'a' is defined by $f(t) = \begin{cases} E, & \text{for } 0 < t < \frac{a}{2} \\ -E, & \text{for } \frac{a}{2} < t < a \end{cases}$ then show that $L\{f(t)\} = \frac{E}{S} \tanh\left(\frac{as}{4}\right)$. (07 Marks)
- c. Using convolution theorem find the inverse Laplace transform of $\frac{s}{(s+2)(s^2+9)}$. (07 Marks)

OR

- 2
- a. Express the function $f(t) = \begin{cases} \cos t & \text{for } 0 < t < \pi \\ \cos 2t & \text{for } \pi < t < 2\pi \\ \cos 3t & \text{for } t > 2\pi \end{cases}$ in terms of unit step function and hence find its Laplace transform. (07 Marks)
- b. Find the inverse Laplace transform of $\frac{2s^2 - 6s + 5}{s^3 - 6s^2 + 11s - 6}$. (06 Marks)
- c. Solve the differential equation $\frac{d^2y}{dt^2} + 4\frac{dy}{dt} + 4y = e^{-t}$ with $y(0) = y'(0) = 0$ by using Laplace transform. (07 Marks)

Module-2

- 3
- a. Find a Fourier series to represent $f(x) = |x|$ in $-\pi \leq x \leq \pi$. (06 Marks)
- b. Obtain the half-range cosine series for $f(x) = x \sin x$ in $(0, \pi)$ and hence show that $\frac{\pi-2}{4} = \frac{1}{1.3} - \frac{1}{3.5} + \frac{1}{5.7} - \dots \dots \infty$ (07 Marks)
- c. Express y as a Fourier series up to second harmonics for the following data :

x:	0	$\frac{\pi}{3}$	$\frac{2\pi}{3}$	π	$\frac{4\pi}{3}$	$\frac{5\pi}{3}$	2π
y:	1	1.4	1.9	1.7	1.5	1.2	1.0

(07 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
2. Any revealing of identification, appeal to evaluator and/or equations written eg, 42+8 = 50, will be treated as malpractice.

OR

- 4 a. Obtain the Fourier series expansion for the function, $f(x) = 2x - x^2$ in $(0, 2)$. (06 Marks)
- b. Find the half range sine series for the function, $f(x) = \begin{cases} \frac{1}{4} - x & \text{for } 0 < x < \frac{1}{2} \\ x - \frac{3}{4} & \text{for } \frac{1}{2} < x < 1 \end{cases}$ (07 Marks)
- c. The following table gives the variation of periodic current over period :

t sec :	0	$\frac{T}{6}$	$\frac{T}{3}$	$\frac{T}{2}$	$\frac{2T}{3}$	$\frac{5T}{6}$	T
A (amp) :	1.98	1.30	1.05	1.30	-0.88	-0.25	1.98

Show that there is a direct current part of 0.75 amp in the variable current and obtain the amplitude of the first harmonic. (07 Marks)

Module-3

- 5 a. Find the Fourier transform of the function $f(x) = \begin{cases} 1 - x^2 & \text{for } |x| \leq 1 \\ 0 & \text{for } |x| > 1 \end{cases}$. Hence evaluate

$$\int_0^{\infty} \left(\frac{x \cos x - \sin x}{x^3} \right) dx. \quad (06 \text{ Marks})$$

- b. Find the Fourier sine and cosine transform of $f(x) = \begin{cases} x & \text{if } 0 < x < 1 \\ 2 - x & \text{if } 1 < x < 2 \\ 0 & \text{otherwise} \end{cases}$. (07 Marks)

- c. Find the z-transform of $\cosh\left(n \frac{\pi}{2} + \theta\right)$. (07 Marks)

OR

- 6 a. Find the Fourier sine transform of $f(x) = e^{-ax}$, $a > 0$. (06 Marks)
- b. Find the inverse z transform of $\frac{18z^2}{(2z-1)(4z+1)}$. (07 Marks)
- c. Solve the difference equation $u_{n+2} + 6u_{n+1} + 9u_n = z^n$ with $u_0 = u_1 = 0$ using z-transform. (07 Marks)

Module-4

- 7 a. Classify the following partial differential equations :

(i) $\frac{\partial^2 u}{\partial x^2} + 4 \frac{\partial^2 u}{\partial x \partial y} + 4 \frac{\partial^2 u}{\partial y^2} - \frac{\partial u}{\partial x} + 2 \frac{\partial u}{\partial y} = 0$.

(ii) $x^2 \frac{\partial^2 u}{\partial x^2} + (1 - y^2) \frac{\partial^2 u}{\partial y^2} = 0$, $-\infty < x < \infty$, $-1 < y < 1$.

(iii) $(1 + x^2) \frac{\partial^2 u}{\partial x^2} + (5 + 2x^2) \frac{\partial^2 u}{\partial x \partial t} + (4 + x^2) \frac{\partial^2 u}{\partial t^2} = 0$.

(iv) $(x + 1) \frac{\partial^2 u}{\partial x^2} - 2(x + 2) \frac{\partial^2 u}{\partial x \partial y} + (x + 3) \frac{\partial^2 u}{\partial y^2} = 0$. (10 Marks)

- b. Evaluate the values at the mesh points for the equation $u_{tt} = 16u_{xx}$ taking $h = 1$ upto $t = 1.25$. The boundary conditions are $u(0, t) = u(5, t) = 0$ and the initial conditions are $u(x, 0) = x^2(5 - x)$ and $u_t(x, 0) = 0$. (10 Marks)

OR

- 8 a. Using Schmidt two-level formula to solve the equation $\frac{\partial^2 u}{\partial x^2} = \frac{\partial u}{\partial t}$ under the conditions,
- (i) $u(0, t) = u(1, t) = 0 \quad t \geq 0$
 - (ii) $u(x, 0) = \sin \pi x, \quad 0 < x < 1$ by taking $h = \frac{1}{4}$ and $\alpha = \frac{1}{6}$ co. (10 Marks)
- b. Solve the two-dimensional Laplace equation $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$ at the interior mesh points of the square region and the values of u at the mesh points on the boundary are shown in Fig.Q8 (b).

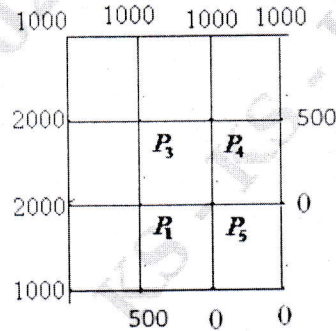


Fig. Q8 (b)

(10 Marks)

Module-5

- 9 a. Using Runge-Kutta method of 4th order to solve the differential equation $\frac{d^2 y}{dx^2} + 2x \frac{dy}{dx} - 4y = 0$ with $y(0) = 0.2$ and $y'(0) = 0.5$ for $x = 0.1$. Correct to four decimal places. (07 Marks)
- b. State and prove Euler's equation. (07 Marks)
- c. Find the extremal of the functional $I = \int_0^{\frac{\pi}{2}} (y^2 - y'^2 - 2y \sin x) dx$ under the end conditions $y(0) = 0, y\left(\frac{\pi}{2}\right) = 0$ (06 Marks)

OR

- 10 a. Apply Milne's method to compute $y(0.3)$. Given that $\frac{d^2 y}{dx^2} = 1 - 2y \frac{dy}{dx}$ and $y(0) = 0, y(0.2) = 0.02, y(0.4) = 0.0795, y(0.6) = 0.1762, y'(0) = 0, y'(0.2) = 0.1996, y'(0.4) = 0.3937, y'(0.6) = 0.5689$ (07 Marks)
- b. Prove that the shortest distance between two points in a plane is a straight line. (07 Marks)
- c. Find the extremal of the functional $I = \int_{x_1}^{x_2} (y^2 + y'^2 + 2ye^x) dx$ (06 Marks)

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21EC32

Third Semester B.E. Degree Examination, Dec.2023/Jan.2024 Digital System Design using Verilog

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Define the following terms with an example
 - (i) Maxterms
 - (ii) Miniterms
 - (iii) Combinational logic circuit(06 Marks)
- b. Place the following equations into the proper canonical form:
 - (i) $P = f(a, b, c) = ab' + ac' + bc$
 - (ii) $J = f(A, B, C, D) = (A + B' + C)(A' + D)$(06 Marks)
- c. Design a combinational circuit to output the 2's complement of a 4-bit binary number. (08 Marks)

OR

- 2 a. Simplify the following Boolean function by using Q.M. method:
 $S = f(w, x, y, z) = \sum(1, 3, 13, 15) + \sum d(8, 9, 10, 11)$ (08 Marks)
- b. Obtain the simplified expression for the given four-variable equation using K-map and identify prime implicant and essential prime implicant.
 $K = f(w, x, y, z) = \sum(0, 1, 4, 5, 9, 11, 13, 15)$ (06 Marks)
- c. Explain briefly K-map, incompletely specified functions, essential prime implicants. (06 Marks)

Module-2

- 3 a. Implement $f(a, b, c, d) = \sum m(0, 1, 5, 6, 7, 9, 10, 15)$ using:
 - i) 8 : 1 MUX with a, b, c as select lines
 - ii) 4 : 1 MUX with a, b as select lines(08 Marks)
- b. Explain the carry look ahead adder with necessary diagram and relevant expressions. (06 Marks)
- c. Design 4:2 line priority encoder which gives MSB the highest priority and LSB least priority. (06 Marks)

OR

- 4 a. Design 2-bit comparator using gates. (08 Marks)
- b. Explain the structure of programmable logic arrays with an example. (06 Marks)
- c. List the applications of decoder. Implement a full adder circuit using 3:8 decoder. (06 Marks)

Module-3

- 5 a. Explain Master-Slave SR flipflop with necessary truth table and timing waveforms. (06 Marks)
- b. Find characteristic equations for J-K and T flip-flops with the help of function tables. (06 Marks)
- c. Describe with neat diagrams the working and truth table of twisted ring counter and Mod-4 ring counter. (08 Marks)

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OR

- 6 a. Explain serial-in serial out and serial-in parallel out unidirectional shift register with neat diagrams. (06 Marks)
b. Explain 4 bit synchronous binary counter with necessary timing waveforms. (06 Marks)
c. Design a synchronous Mod-6 counter using clocked JK flipflops. (08 Marks)

Module-4

- 7 a. Describe the structure of the verilog module with an example. (06 Marks)
b. Briefly explain the different data types in verilog. (08 Marks)
c. Write a verilog data flow description for full adder circuit. (06 Marks)

OR

- 8 a. Write a verilog code for 2:1 multiplexer with active low enable. (06 Marks)
b. Explain with an example how signal declaration and constant declaration is done in verilog. (06 Marks)
c. Discuss the shift operators and bitwise logical operators in verilog with examples. (08 Marks)

Module-5

- 9 a. Explain if-else structure and design a behavioral description of a D-latch using if statement. (06 Marks)
b. Realize 3:8 decoder using verilog behavioral description. (06 Marks)
c. Write a verilog description of a 4 × 4 bit Booth algorithm. (08 Marks)

OR

- 10 a. Write a structural description of a Half adder by describing the built in gates in verilog. (06 Marks)
b. Write a verilog structural description of ripple carry adder. (06 Marks)
c. Realize binary up/down counter using verilog behavioral description. (08 Marks)

CBCS SCHEME

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21EC33

Third Semester B.E. Degree Examination, Dec.2023/Jan.2024 Basic Signal Processing

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Write the complete solution $x = x_p + x_n$ to

$$A = \begin{bmatrix} 1 & 2 & 2 & 2 \\ 2 & 4 & 6 & 8 \\ 3 & 6 & 8 & 10 \end{bmatrix}$$

(10 Marks)

- b. Define the four fundamental vector spaces and find the Dimension and basis for four fundamental subspaces for :

$$A = \begin{bmatrix} 1 & 2 & 3 & 5 \\ 2 & 4 & 8 & 12 \\ 3 & 6 & 7 & 13 \end{bmatrix}$$

(10 Marks)

OR

- 2 a. Illustrate the transformation of the plane that comes from four matrices and list the transformations $T(x)$ that are not possible with Ax . (10 Marks)

- b. Compute $A^T A$ and their eigen values and unit eigen vectors for V and u . Then check $AV = u\Sigma$.

$$A = \begin{bmatrix} 1 & 1 \\ 0 & 1 \\ -1 & 1 \end{bmatrix}$$

(10 Marks)

Module-2

- 3 a. What is an orthogonal matrix. Apply the gram Schmidt process to

$$a = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \quad b = \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} \quad c = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$$

and write the result in the form of $A = QR$.

(10 Marks)

- b. Find the projection of b onto the column space of A .

$$A = \begin{bmatrix} 1 & 1 \\ 1 & -1 \\ -2 & 4 \end{bmatrix} \quad b = \begin{bmatrix} 1 \\ 2 \\ 7 \end{bmatrix}$$

(10 Marks)

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OR

- 4 a. Find eigen values and eigen vectors for the matrix. A can the matrix be diagonalized. (10 Marks)

$$A = \begin{bmatrix} 1 & 6 & 1 \\ 1 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$$

- b. i) What is a positive definite matrix? Mention the methods of testing positive definiteness. (04 Marks)

ii) Decide for or against the positive definiteness of

$$A = \begin{bmatrix} 2 & -1 & -1 \\ -1 & 2 & -1 \\ -1 & -1 & 2 \end{bmatrix} \quad B = \begin{bmatrix} 2 & -1 & -1 \\ -1 & 2 & 1 \\ -1 & 1 & 2 \end{bmatrix}$$

(06 Marks)

Module-3

- 5 a. Define a signal. List the elementary signals. Differentiate between even and odd signals, energy and power signals. (10 Marks)

- b. Sketch the even the odd part of the signals shown in Fig.Q5(b)(i) and 5(b)(ii).

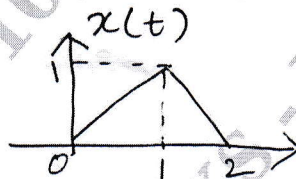


Fig.Q5(b)(i)

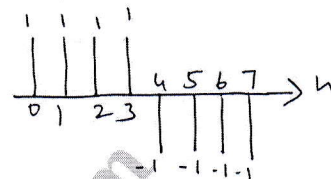


Fig.Q5(b)(ii)

(08 Marks)

- c. Determine whether the following signal is periodic or not. If periodic find the fundamental period $x(n) = \cos\left(\frac{n\pi}{5}\right)\sin\left(\frac{n\pi}{3}\right)$. (02 Marks)

OR

- 6 a. Determine whether the following systems are memoryless, causal time invariant, linear and stable. i) $y(n) = nx(n)$ ii) $y(t) = x(t/2)$. (08 Marks)

- b. For the signal $x(t)$ and $y(t)$ shown in Fig.6(a) sketch the following signals :

- i) $x(t+1)y(t-2)$ ii) $x(t)y(t-1)$

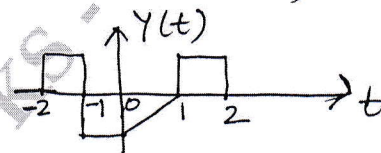
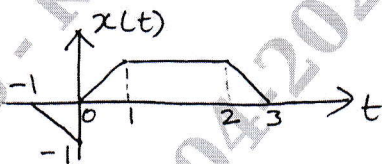


Fig.Q6(b)

(08 Marks)

- c. Sketch the waveform of the signal : $x(t) = u(t+1) - 2u(t) + u(t-1)$. (04 Marks)

Module-4

- 7 a. Compute the following convolution :

i) $y(t) = e^{-2t}u(t-2) * \{u(t-2) - u(t-12)\}$

ii) $y(n) = \alpha^n \{u(n) - u(n-6)\} * 2\{u(n) - 4u(n-15)\}$. (14 Marks)

- b. Prove the following :

i) $x(t) * \delta(t-t_0) = x(t-t_0)$

ii) $x(n) * u(n) = \sum_{k=-\infty}^n X(k)$. (06 Marks)

OR

- 8 a. Evaluate the step response for LTI system represented by the following impulse response :
- i) $h(t) = u(t + 1) - u(t - 1)$
 - ii) $h(n) = (1/2)^n u(n)$. (08 Marks)
- b. Determine whether the following system defined by their impulse response are causes memoryless and stable.
- i) $h(t) = e^{-2t} u(t - 1)$
 - ii) $h(n) = 2u(n) - 2u(n - 5)$. (08 Marks)
- c. A system consists of several subsystems connected as shown in Fig.Q8(c). Find the operator H relating $x(t)$ to $y(t)$ for the following subsystem operators.
- H1 : $Y_1(t) = X_1(t)X_1(t - 1)$
 - H2 : $Y_2(t) = |X_2(t)|$
 - H3 : $Y_3(t) = 1 + 2 X_3(t)$
 - H4 : $Y_4(t) = \cos(X_4(t))$.

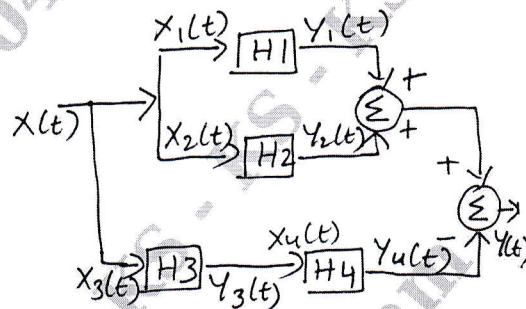


Fig.Q8(c)

(04 Marks)

Module-5

- 9 a. Describe the properties of region of convergence and sketch the ROL of two sided, right sided and left sided sequence. (08 Marks)
- b. Find Z – transform of the following and specify its ROC
- $x(n) = \sin\left(\frac{\pi}{4}n - \frac{\pi}{2}\right) u(n - 2)$
 - $x(n) = \left(\frac{2}{3}\right)^n u(n) * 2^n u(-n - 3)$. (08 Marks)
- c. Find inverse Z-transform if $X(z) = \frac{(1/4)z^{-1}}{(1 - 1/2 z^{-1})(1 - 1/4 z^{-1})}$. (04 Marks)

OR

- 10 a. Describe the transfer function and the impulse response for the causal LTI system described by the differential equation :
- $$y(n) - \frac{1}{4}y(n - 1) - \frac{3}{8}y(n - 2) = -x(n) + 2x(n - 1)$$
- (10 Marks)
- b. Determine the impulse response of the following transfer function if :
- i) The system is causal
 - ii) The system is stable
 - iii) The system is stable and causal at the same time : $H(z) = \frac{3z^{+2} - z}{(z - 2)\left(z + \frac{1}{2}\right)}$. (10 Marks)

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Third Semester B.E. Degree Examination, Dec.2023/Jan.2024 Analog Electronic Circuits

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Explain biasing of BJT by collector to base feedback resistor for a CE amplifier. (08 Marks)
- b. A BJT having $\beta = 100$ is biased at a DC collector current of 1 mA. Find the value of g_m , r_e , r_π at the bias point. Assume $V_T = \frac{1}{40}$ V. (04 Marks)
- c. Draw the small signal equivalent circuit model for MOSFET and obtain the expression for voltage gain. (08 Marks)

OR

- 2 a. Explain biasing of MOSFET using drain to gate feedback resistor. (06 Marks)
- b. What is transconductance of a MOSFET and mention the three different expression used to calculate the g_m . (06 Marks)
- c. For the circuit shown in Fig. Q2 (c), find the required value of V_{GS} to establish a dc bias current $I_D = 0.5$ mA. Device parameters are $V_t = 1$ V, $K'_n \frac{W}{L} = 1$ mA/V² and $\lambda = 0$. What is the percentage change in I_D obtained when the transistor is replaced with another having $V_t = 1.5$ V. (08 Marks)

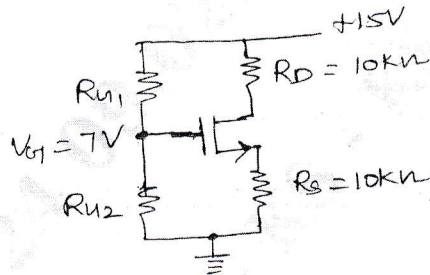


Fig. Q2 (c)

Module-2

- 3 a. With mathematical equations, explain the different internal capacitances in the MOSFET. (10 Marks)
- b. Explain the high frequency response of a CS amplifier using MOSFET and derive its upper cut off frequency. (10 Marks)

OR

- 4 a. Draw the circuit of a RC phase shift oscillator using MOSFET and explain the working. (06 Marks)
- b. A 2 MHz quartz crystal is specified to have $L = 0.52$ H, $C_S = 0.012$ PF, $C_P = 4$ PF and $R = 120$ Ω. Find f_s , f_p . (04 Marks)
- c. Derive the expression of R_{in} , R_O , A_{VO} and A_V using T model for the common source amplifier with a source resistance circuit. (10 Marks)

Module-3

- 5 a. What are the properties of negative feedback and explain it briefly. (10 Marks)
 b. What are the topologies of basic feedback circuit? (04 Marks)
 c. For the block diagram, shown in Fig. Q5 (c), a signal of 1 V from the source results in a difference signal of 10 mV being provided to the amplifier (A) and 10 V applied to the load. For this arrangement identify the value of A and β that apply. (06 Marks)

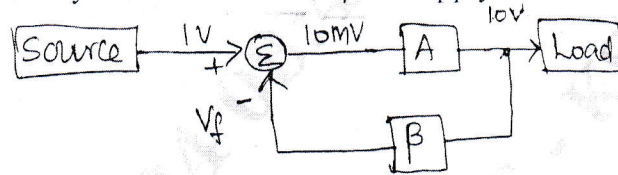


Fig. Q5 (c)

OR

- 6 a. Draw the circuit of a transformer coupled class-A power amplifier. Prove that the maximum conversion efficiency is 50%. (08 Marks)
 b. What is output stage and discuss the classification of output stages based on the collector current? (06 Marks)
 c. Neatly draw the schematic diagram of class C tuned amplifier and discuss the input and output waveforms at the collector terminal. (06 Marks)

Module-4

- 7 a. Derive the expression of output voltage and explain the operation of 4-bit DAC using R-2R circuit. (10 Marks)
 b. What is meant by precision rectification? Explain with a neat circuit diagram, the working of a small signal half wave precision rectifier using Op-Amp. (10 Marks)

OR

- 8 a. With the help of a neat circuit diagram and relevant waveforms, explain the working of astable multivibrator circuit operation using 555 timer IC. Derive expression for T_{ON} , T_{OFF} and T. (10 Marks)
 b. Explain the working of a second order lowpass butterworth filter. Write the design equations. Design the circuit for cut off frequency of 1 kHz. (10 Marks)

Module-5

- 9 a. With the help of the static V-I characteristics, explain the three modes of operation of the thyristor. (10 Marks)
 b. Explain the working of a UJT firing circuit using SCR with necessary circuit diagram and waveforms. (10 Marks)

OR

- 10 a. Discuss various power converter circuits with necessary sketches and applications of each. (08 Marks)
 b. List different turn on methods, explain all in brief. (08 Marks)
 c. Enumerate the applications of power electronics. (04 Marks)

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