

CBCS SCHEME

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16/17SCS23

Second Semester M.Tech. Degree Examination, June/July 2019 Advanced Algorithms

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Explain the various types of asymptotic notations with an example. (08 Marks)
b. What is recurrence? Solve the recurrence using substitution method.

$$T(n) = \begin{cases} 1, & \text{if } n = 1 \\ 2T\left(\frac{n}{2}\right) + n, & \text{if } n > 1 \end{cases} \quad (08 \text{ Marks})$$

OR

- 2 a. Use recursion tree method to solve the recurrence $T(n) = 3T\left(\frac{n}{4}\right) + Cn^2$. (06 Marks)
b. State the Master theorem and solve the following recurrence relations using Master theorem.
 $T(n) = 3T\left(\frac{n}{4}\right) + n \lg n$. (04 Marks)
c. What is amortized analysis? What are the common techniques used in amortized analysis? Explain any two techniques with an example. (06 Marks)

Module-2

- 3 a. Using Bellman – Ford algorithm, find the shortest path from the source vertex '5' to the remaining vertices in the graph shown in the Fig.Q3(a). (08 Marks)

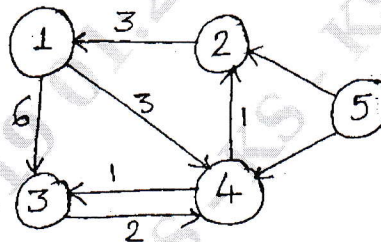


Fig.Q3(a)

- b. Write the Johnson's algorithm to solve all - pair shortest path problem for sparse graphs with example. (08 Marks)

OR

- 4 a. Write and explain the algorithm for recursive FFT. Also determine its running time. (08 Marks)
b. Explain Ford–Fulkerson method for solving the maximum flow problem. (08 Marks)

Module-3

- 5 a. Write Extended Euclid algorithm and compute the values (d, x, y) that call the Extended_Euclid(299, 221). (08 Marks)
b. Write and explain algorithm to solve modular linear equation. Also find all solutions to the equation: $35x \equiv 50 \pmod{55}$. (08 Marks)

OR

- 6 a. Use Chinese remainder theorem to find all solutions to the equation : $x \equiv 3 \pmod{5}$ and $x \equiv 4 \pmod{7}$. (08 Marks)
- b. Consider an RSA key set with $p = 11$, $q = 29$, $n = 319$ and $e = 3$, what value of 'd' should be used in the secret key? What is the encryption of the message $M = 100$? (08 Marks)

Module-4

- 7 a. Write and explain the Rabin-Karp string matching algorithm. working modulo $q = 11$, how many spurious hits does the Rabin-Karp matcher encounter in the text : $T = 3\ 1\ 4\ 1\ 5\ 9\ 2\ 6\ 5\ 3\ 5\ 8\ 9\ 7\ 9\ 3$ when looking for the pattern $p = 26$? (08 Marks)
- b. Construct the string matching automation for the pattern $p = a\ a\ b\ a\ b$ and illustrate its operation on the text string $T = a\ a\ a\ b\ a\ b\ a\ b\ a\ a\ b\ a\ b\ a\ a\ b$. (08 Marks)

OR

- 8 a. Write the Knuth – Morris – Pratt algorithm for string matching. Compute the prefix function π for the pattern $a\ b\ a\ b\ b\ a\ b\ b\ a\ b\ b\ a\ b\ a\ b\ b\ a\ b\ b$. (08 Marks)
- b. Write the Naïve string matching algorithm. Show the operation of the same, for the pattern in the text $T = 0\ 0\ 0\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 1\ 0\ 0\ 0\ 1$. (08 Marks)

Module-5

- 9 a. Explain randomizing deterministic algorithms taking linear search algorithm as an example. (08 Marks)
- b. Write an algorithm for testing polynomial equality using Monte Carlo algorithm (08 Marks)

OR

- 10 a. Explain Monte Carlo and Las Vegas algorithms wit appropriate examples. (08 Marks)
- b. Write a note on probabilistic numerical algorithms. (08 Marks)
